

NAG Fortran Library Routine Document

G02HAF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of *bold italicised* terms and other implementation-dependent details.

1 Purpose

G02HAF performs bounded influence regression (M-estimates). Several standard methods are available.

2 Specification

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SUBROUTINE G02HAF (INDW, IPSI, ISIGMA, INDC, N, M, X, IX, Y, CPSI, H1,
1 H2, H3, CUCV, DCHI, THETA, SIGMA, C, IC, RS, WGT,
2 TOL, MAXIT, NITMON, WORK, IFAIL)

INTEGER INDW, IPSI, ISIGMA, INDC, N, M, IX, IC, MAXIT,
1 NITMON, IFAIL
double precision X(IX,M), Y(N), CPSI, H1, H2, H3, CUCV, DCHI,
1 THETA(M), SIGMA, C(IC,M), RS(N), WGT(N), TOL,
2 WORK(4*N+M*(N+M))

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3 Description

For the linear regression model

$$y = X\theta + \epsilon,$$

where y is a vector of length n of the dependent variable,

X is a n by m matrix of independent variables of column rank k ,

θ is a vector of length m of unknown parameters,

and ϵ is a vector of length n of unknown errors with $\text{var}(\epsilon_i) = \sigma^2$,

G02HAF calculates the M-estimates given by the solution, $\hat{\theta}$, to the equation

$$\sum_{i=1}^n \psi(r_i/(\sigma w_i)) w_i x_{ij} = 0, \quad j = 1, 2, \dots, m, \quad (1)$$

where r_i is the i th residual, i.e., the i th element of $r = y - X\hat{\theta}$,

ψ is a suitable weight function,

w_i are suitable weights,

and σ may be estimated at each iteration by the median absolute deviation of the residuals

$$\hat{\sigma} = \text{med}_i [|r_i|] / \beta_1$$

or as the solution to

$$\sum_{i=1}^n \chi(r_i/(\hat{\sigma} w_i)) w_i^2 = (n - k) \beta_2$$

for suitable weight function χ , where β_1 and β_2 are constants, chosen so that the estimator of σ is asymptotically unbiased if the errors, ϵ_i , have a Normal distribution. Alternatively σ may be held at a constant value.

The above describes the Schweppe type regression. If the w_i are assumed to equal 1 for all i then Huber type regression is obtained. A third type, due to Mallows, replaces (1) by

$$\sum_{i=1}^n \psi(r_i/\sigma) w_i x_{ij} = 0, \quad j = 1, 2, \dots, m.$$

This may be obtained by use of the transformations

$$\begin{aligned} w_i^* &\leftarrow \sqrt{w_i} \\ y_i^* &\leftarrow y_i \sqrt{w_i} \\ x_{ij}^* &\leftarrow x_{ij} \sqrt{w_i}, \quad j = 1, 2, \dots, m \end{aligned}$$

(see Section 3 of Marazzi (1987a)).

For Huber and Schweppe type regressions, β_1 is the 75th percentile of the standard Normal distribution. For Mallows type regression β_1 is the solution to

$$\frac{1}{n} \sum_{i=1}^n \Phi(\beta_1/\sqrt{w_i}) = 0.75,$$

where Φ is the standard Normal cumulative distribution function (see S15ABF).

β_2 is given by

$$\beta_2 = \int_{-\infty}^{\infty} \chi(z) \phi(z) dz \quad \text{in the Huber case;}$$

$$\beta_2 = \frac{1}{n} \sum_{i=1}^n w_i \int_{-\infty}^{\infty} \chi(z) \phi(z) dz \quad \text{in the Mallows case;}$$

$$\beta_2 = \frac{1}{n} \sum_{i=1}^n w_i^2 \int_{-\infty}^{\infty} \chi(z/w_i) \phi(z) dz \quad \text{in the Schweppe case;}$$

where ϕ is the standard Normal density, i.e., $\frac{1}{\sqrt{2\pi}} \exp(-\frac{1}{2}x^2)$.

The calculation of the estimates of θ can be formulated as an iterative weighted least-squares problem with a diagonal weight matrix G given by

$$G_{ii} = \begin{cases} \frac{\psi(r_i/(\sigma w_i))}{(r_i/(\sigma w_i))}, & r_i \neq 0 \\ \psi'(0), & r_i = 0 \end{cases},$$

where $\psi'(t)$ is the derivative of ψ at the point t .

The value of θ at each iteration is given by the weighted least-squares regression of y on X . This is carried out by first transforming the y and X by

$$\begin{aligned} \tilde{y}_i &= y_i \sqrt{G_{ii}} \\ \tilde{x}_{ij} &= x_{ij} \sqrt{G_{ii}}, \quad j = 1, 2, \dots, m \end{aligned}$$

and then using F04JGF. If X is of full column rank then an orthogonal-triangular (QR) decomposition is used; if not, a singular value decomposition is used.

The following functions are available for ψ and χ in G02HAF.

(a) **Unit Weights**

$$\psi(t) = t, \quad \chi(t) = \frac{t^2}{2}.$$

This gives least-squares regression.

(b) Huber's Function

$$\psi(t) = \max(-c, \min(c, t)), \quad \chi(t) = \begin{cases} \frac{t^2}{2}, & |t| \leq d \\ \frac{d^2}{2}, & |t| > d \end{cases}$$

(c) Hampel's Piecewise Linear Function

$$\psi_{h_1, h_2, h_3}(t) = -\psi_{h_1, h_2, h_3}(-t) = \begin{cases} t, & 0 \leq t \leq h_1 \\ h_1, & h_1 \leq t \leq h_2 \\ h_1(h_3 - t)/(h_3 - h_2), & h_2 \leq t \leq h_3 \\ 0, & h_3 < t \end{cases}$$

$$\chi(t) = \begin{cases} \frac{t^2}{2}, & |t| \leq d \\ \frac{d^2}{2}, & |t| > d \end{cases}$$

(d) Andrew's Sine Wave Function

$$\psi(t) = \begin{cases} \sin t, & -\pi \leq t \leq \pi \\ 0, & |t| > \pi \end{cases} \quad \chi(t) = \begin{cases} \frac{t^2}{2}, & |t| \leq d \\ \frac{d^2}{2}, & |t| > d \end{cases}$$

(e) Tukey's Bi-weight

$$\psi(t) = \begin{cases} t(1 - t^2)^2, & |t| \leq 1 \\ 0, & |t| > 1 \end{cases} \quad \chi(t) = \begin{cases} \frac{t^2}{2}, & |t| \leq d \\ \frac{d^2}{2}, & |t| > d \end{cases}$$

where c , h_1 , h_2 , h_3 , and d are given constants.

Several schemes for calculating weights have been proposed, see Hampel *et al.* (1986) and Marazzi (1987a). As the different independent variables may be measured on different scales, one group of proposed weights aims to bound a standardized measure of influence. To obtain such weights the matrix A has to be found such that:

$$\frac{1}{n} \sum_{i=1}^n u(\|z_i\|_2) z_i z_i^T = I$$

and

$$z_i = Ax_i,$$

where x_i is a vector of length m containing the i th row of X ,

A is an m by m lower triangular matrix,

and u is a suitable function.

The weights are then calculated as

$$w_i = f(\|z_i\|_2)$$

for a suitable function f .

G02HAF finds A using the iterative procedure

$$A_k = (S_k + I)A_{k-1},$$

where $S_k = (s_{jl})$,

$$s_{jl} = \begin{cases} -\min[\max(h_{jl}/n, -BL), BL], & j > 1 \\ -\min[\max(\frac{1}{2}(h_{jj}/n - 1), -BD), BD], & j = 1 \end{cases}$$

and

$$h_{jl} = \sum_{i=1}^n u(\|z_i\|_2) z_{ij} z_{il}$$

and BL and BD are bounds set at 0.9.

Two weights are available in G02HAF:

(i) **Krasker–Welsch Weights**

$$u(t) = g_1\left(\frac{c}{t}\right),$$

where $g_1(t) = t^2 + (1 - t^2)(2\Phi(t) - 1) - 2t\phi(t)$,

$\Phi(t)$ is the standard Normal cumulative distribution function,

$\phi(t)$ is the standard Normal probability density function,

and $f(t) = \frac{1}{t}$.

These are for use with Schweppe type regression.

(ii) **Maronna's Proposed Weights**

$$u(t) = \begin{cases} \frac{c}{t^2} & |t| > c \\ 1 & |t| \leq c \end{cases}$$

$$f(t) = \sqrt{u(t)}.$$

These are for use with Mallows type regression.

Finally the asymptotic variance-covariance matrix, C , of the estimates θ is calculated.

For Huber type regression

$$C = f_H (X^T X)^{-1} \hat{\sigma}^2,$$

where

$$f_H = \frac{1}{n - m} \frac{\sum_{i=1}^n \psi^2(r_i/\hat{\sigma})}{\left(\frac{1}{n} \sum_{i=1}^n \psi'(r_i/\hat{\sigma})\right)^2 \kappa^2}$$

$$\kappa^2 = 1 + \frac{m}{n} \frac{\frac{1}{n} \sum_{i=1}^n \left(\psi'(r_i/\hat{\sigma}) - \frac{1}{n} \sum_{i=1}^n \psi'(r_i/\hat{\sigma})\right)^2}{\left(\frac{1}{n} \sum_{i=1}^n \psi'(r_i/\hat{\sigma})\right)^2}.$$

See Huber (1981) and Marazzi (1987b).

For Mallows and Schweppe type regressions C is of the form

$$\frac{\hat{\sigma}^2}{n} S_1^{-1} S_2 S_1^{-1},$$

where $S_1 = \frac{1}{n} X^T D X$ and $S_2 = \frac{1}{n} X^T P X$.

D is a diagonal matrix such that the i th element approximates $E(\psi'(r_i/(\sigma w_i)))$ in the Schweppe case and $E(\psi'(r_i/\sigma)w_i)$ in the Mallows case.

P is a diagonal matrix such that the i th element approximates $E(\psi^2(r_i/(\sigma w_i))w_i^2)$ in the Schweppe case and $E(\psi^2(r_i/\sigma)w_i^2)$ in the Mallows case.

Two approximations are available in G02HAF:

1. Average over the r_i

Schweppe	Mallows
$D_i = \left(\frac{1}{n} \sum_{j=1}^n \psi' \left(\frac{r_j}{\sigma w_i} \right) \right) w_i$	$D_i = \left(\frac{1}{n} \sum_{j=1}^n \psi' \left(\frac{r_j}{\sigma} \right) \right) w_i$
$P_i = \left(\frac{1}{n} \sum_{j=1}^n \psi^2 \left(\frac{r_j}{\sigma w_i} \right) \right) w_i^2$	$P_i = \left(\frac{1}{n} \sum_{j=1}^n \psi^2 \left(\frac{r_j}{\sigma} \right) \right) w_i^2$

2. Replace expected value by observed

Schweppe	Mallows
$D_i = \psi' \left(\frac{r_i}{\sigma w_i} \right) w_i$	$D_i = \psi' \left(\frac{r_i}{\sigma} \right) w_i$
$P_i = \psi^2 \left(\frac{r_i}{\sigma w_i} \right) w_i^2$	$P_i = \psi^2 \left(\frac{r_i}{\sigma} \right) w_i^2$

See Hampel *et al.* (1986) and Marazzi (1987b).

Note: there is no explicit provision in the routine for a constant term in the regression model. However, the addition of a dummy variable whose value is 1.0 for all observations will produce a value of $\hat{\theta}$ corresponding to the usual constant term.

G02HAF is based on routines in ROBETH; see Marazzi (1987a).

4 References

Hampel F R, Ronchetti E M, Rousseeuw P J and Stahel W A (1986) *Robust Statistics. The Approach Based on Influence Functions* Wiley

Huber P J (1981) *Robust Statistics* Wiley

Marazzi A (1987a) Weights for bounded influence regression in ROBETH *Cah. Rech. Doc. IUMSP, No. 3 ROB 3* Institut Universitaire de Médecine Sociale et Préventive, Lausanne

Marazzi A (1987b) Subroutines for robust and bounded influence regression in ROBETH *Cah. Rech. Doc. IUMSP, No. 3 ROB 2* Institut Universitaire de Médecine Sociale et Préventive, Lausanne

5 Parameters

1: INDW – INTEGER

Input

On entry: specifies the type of regression to be performed.

INDW = 0

Huber type regression.

INDW < 0

Mallows type regression with Maronna's proposed weights.

INDW > 0

Schweppe type regression with Krasker–Welsch weights.

2: IPSI – INTEGER *Input*

On entry: specifies which ψ function is to be used.

IPSI = 0

$\psi(t) = t$, i.e., least-squares.

IPSI = 1

Huber's function.

IPSI = 2

Hampel's piecewise linear function.

IPSI = 3

Andrew's sine wave.

IPSI = 4

Tukey's bi-weight.

Constraint: $0 \leq \text{IPSI} \leq 4$.

3: ISIGMA – INTEGER *Input*

On entry: specifies how σ is to be estimated.

ISIGMA < 0

σ is estimated by median absolute deviation of residuals.

ISIGMA = 0

σ is held constant at its initial value.

ISIGMA > 0

σ is estimated using the χ function.

4: INDC – INTEGER *Input*

On entry: if INDW $\neq 0$, INDC specifies the approximations used in estimating the covariance matrix of $\hat{\theta}$.

INDC = 1

Averaging over residuals.

INDC $\neq 1$

Replacing expected by observed.

INDW = 0

INDC is not referenced.

5: N – INTEGER *Input*

On entry: n , the number of observations.

Constraint: $N > 1$.

- 6: M – INTEGER *Input*
On entry: m , the number of independent variables.
Constraint: $1 \leq M < N$.
- 7: X(IX,M) – **double precision** array *Input/Output*
On entry: the values of the X matrix, i.e., the independent variables. $X(i,j)$ must contain the ij th element of X , for $i = 1, 2, \dots, n$; $j = 1, 2, \dots, m$.
 If $INDW < 0$, then during calculations the elements of X will be transformed as described in Section 3. Before exit the inverse transformation will be applied. As a result there may be slight differences between the input X and the output X .
On exit: unchanged, except as described above.
- 8: IX – INTEGER *Input*
On entry: the first dimension of the array X as declared in the (sub)program from which G02HAF is called.
Constraint: $IX \geq N$.
- 9: Y(N) – **double precision** array *Input/Output*
On entry: the data values of the dependent variable.
 $Y(i)$ must contain the value of y for the i th observation, for $i = 1, 2, \dots, n$.
 If $INDW < 0$, then during calculations the elements of Y will be transformed as described in Section 3. Before exit the inverse transformation will be applied. As a result there may be slight differences between the input Y and the output Y .
On exit: unchanged, except as described above.
- 10: CPSI – **double precision** *Input*
On entry: if $IPSI = 1$, CPSI must specify the parameter, c , of Huber's ψ function.
 If $IPSI \neq 1$ on entry, CPSI is not referenced.
Constraint: if $CPSI > 0.0$, $IPSI = 1$.
- 11: H1 – **double precision** *Input*
 12: H2 – **double precision** *Input*
 13: H3 – **double precision** *Input*
On entry: if $IPSI = 2$, H1, H2, and H3 must specify the parameters h_1 , h_2 , and h_3 , of Hampel's piecewise linear ψ function. H1, H2, and H3 are not referenced if $IPSI \neq 2$.
Constraint: if $IPSI = 2$, $0.0 \leq H1 \leq H2 \leq H3$ and $H3 > 0.0$.
- 14: CUCV – **double precision** *Input*
On entry: if $INDW < 0$, must specify the value of the constant, c , of the function u for Maronna's proposed weights.
 If $INDW > 0$, must specify the value of the function u for the Krasker–Welsch weights.
 If $INDW = 0$, is not referenced.
Constraints:
 if $INDW < 0$, $CUCV \geq M$;
 if $INDW > 0$, $CUCV \geq \sqrt{M}$.

- 15: DCHI – *double precision* *Input*
On entry: d , the constant of the χ function. DCHI is not referenced if IPSI = 0, or if ISIGMA \leq 0.
Constraint: if IPSI \neq 0 and ISIGMA $>$ 0, DCHI $>$ 0.0.
- 16: THETA(M) – *double precision* array *Input/Output*
On entry: starting values of the parameter vector θ . These may be obtained from least-squares regression. Alternatively if ISIGMA $<$ 0 and SIGMA = 1 or if ISIGMA $>$ 0 and SIGMA approximately equals the standard deviation of the dependent variable, y , then THETA(i) = 0.0, for $i = 1, 2, \dots, m$ may provide reasonable starting values.
On exit: THETA(i) contains the M-estimate of θ_i , for $i = 1, 2, \dots, m$.
- 17: SIGMA – *double precision* *Input/Output*
On entry: a starting value for the estimation of σ . SIGMA should be approximately the standard deviation of the residuals from the model evaluated at the value of θ given by THETA on entry.
Constraint: SIGMA $>$ 0.0.
On exit: contains the final estimate of σ if ISIGMA \neq 0 or the value assigned on entry if ISIGMA = 0.
- 18: C(IC,M) – *double precision* array *Output*
On exit: the diagonal elements of C contain the estimated asymptotic standard errors of the estimates of θ , i.e., C(i, i) contains the estimated asymptotic standard error of the estimate contained in THETA(i).
 The elements above the diagonal contain the estimated asymptotic correlation between the estimates of θ , i.e., C(i, j), $1 \leq i < j \leq m$ contains the asymptotic correlation between the estimates contained in THETA(i) and THETA(j).
 The elements below the diagonal contain the estimated asymptotic covariance between the estimates of θ , i.e., C(i, j), $1 \leq j < i \leq m$ contains the estimated asymptotic covariance between the estimates contained in THETA(i) and THETA(j).
- 19: IC – INTEGER *Input*
On entry: the first dimension of the array C as declared in the (sub)program from which G02HAF is called.
Constraint: IC \geq M.
- 20: RS(N) – *double precision* array *Output*
On exit: the residuals from the model evaluated at final value of THETA, i.e., RS contains the vector $(y - X\hat{\theta})$.
- 21: WGT(N) – *double precision* array *Output*
On exit: the vector of weights. WGT(i) contains the weight for the i th observation, for $i = 1, 2, \dots, n$.
- 22: TOL – *double precision* *Input*
On entry: the relative precision for the calculation of A (if INDW \neq 0), the estimates of θ and the estimate of σ (if ISIGMA \neq 0). Convergence is assumed when the relative change in all elements being considered is less than TOL.
 If INDW $<$ 0 and ISIGMA $<$ 0, TOL is also used to determine the precision of β_1 .
 It is advisable for TOL to be greater than $100 \times$ *machine precision*.
Constraint: TOL $>$ 0.0.

23: MAXIT – INTEGER

Input

On entry: the maximum number of iterations that should be used in the calculation of A (if $\text{INDW} \neq 0$), and of the estimates of θ and σ , and of β_1 (if $\text{INDW} < 0$ and $\text{ISIGMA} < 0$).

A value of $\text{MAXIT} = 50$ should be adequate for most uses.

Constraint: $\text{MAXIT} > 0$.

24: NITMON – INTEGER

Input

On entry: the amount of information that is printed on each iteration.

$\text{NITMON} = 0$

No information is printed.

$\text{NITMON} \neq 0$

The current estimate of θ , the change in θ during the current iteration and the current value of σ are printed on the first and every $\text{ABS}(\text{NITMON})$ iterations.

Also, if $\text{INDW} \neq 0$ and $\text{NITMON} > 0$ then information on the iterations to calculate A is printed. This is the current estimate of A and the maximum value of S_{ij} (see Section 3).

When printing occurs the output is directed to the current advisory message unit (see X04ABF).

25: $\text{WORK}(4 \times N + M \times (N + M))$ – *double precision* array*Output*

On exit: the following values are assigned to WORK :

$\text{WORK}(1) = \beta_1$ if $\text{ISIGMA} < 0$, or $\text{WORK}(1) = \beta_2$ if $\text{ISIGMA} > 0$.

$\text{WORK}(2) =$ number of iterations used to calculate A .

$\text{WORK}(3) =$ number of iterations used to calculate final estimates of θ and σ .

$\text{WORK}(4) = k$, the rank of the weighted least-squares equations.

The rest of the array is used as workspace.

26: IFAIL – INTEGER

Input/Output

On initial entry: IFAIL must be set to 0, -1 or 1. If you are unfamiliar with this parameter you should refer to Chapter P01 for details.

On final exit: $\text{IFAIL} = 0$ unless the routine detects an error (see Section 6).

For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, because for this routine the values of the output parameters may be useful even if $\text{IFAIL} \neq 0$ on exit, the recommended value is -1 . **When the value -1 or 1 is used it is essential to test the value of IFAIL on exit.**

6 Error Indicators and Warnings

If on entry $\text{IFAIL} = 0$ or -1 , explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

$\text{IFAIL} = 1$

On entry, $N \leq 1$,
 or $M < 1$,
 or $N \leq M$,
 or $\text{IX} < N$,
 or $\text{IC} < M$.

IFAIL = 2

On entry, IPSI < 0,
or IPSI > 4.

IFAIL = 3

On entry, SIGMA \leq 0.0,
or IPSI = 1 and CPSI \leq 0.0,
or IPSI = 2 and H1 < 0.0,
or IPSI = 2 and H1 > H2,
or IPSI = 2 and H2 > H3,
or IPSI = 2 and H1 = H2 = H3 = 0.0,
or IPSI \neq 0 and ISIGMA > 0 and DCHI \leq 0.0,
or INDW > 0 and CUCV < \sqrt{M} ,
or INDW < 0 and CUCV < M.

IFAIL = 4

On entry, TOL \leq 0.0,
or MAXIT \leq 0.

IFAIL = 5

The number of iterations required to calculate the weights exceeds MAXIT. (Only if INDW \neq 0.)

IFAIL = 6

The number of iterations required to calculate β_1 exceeds MAXIT. (Only if INDW < 0 and ISIGMA < 0.)

IFAIL = 7

Either the number of iterations required to calculate θ and σ exceeds MAXIT (note that, in this case WK(3) = MAXIT on exit), or the iterations to solve the weighted least-squares equations failed to converge. The latter is an unlikely error exit.

IFAIL = 8

The weighted least-squares equations are not of full rank.

IFAIL = 9

If INDW = 0 then $(X^T X)$ is almost singular.

If INDW \neq 0 then S_1 is singular or almost singular. This may be due to too many diagonal elements of the matrix being zero, see Section 8.

IFAIL = 10

In calculating the correlation factor for the asymptotic variance-covariance matrix either the value of

$$\frac{1}{n} \sum_{i=1}^n \psi'(r_i/\hat{\sigma}) = 0, \quad \text{or} \quad \kappa = 0, \quad \text{or} \quad \sum_{i=1}^n \psi^2(r_i/\hat{\sigma}) = 0.$$

See Section 8. In this case C is returned as $X^T X$.

(Only if INDW = 0.)

IFAIL = 11

The estimated variance for an element of $\theta \leq 0$.

In this case the diagonal element of C will contain the negative variance and the above diagonal elements in the row and column corresponding to the element will be returned as zero.

This error may be caused by rounding errors or too many of the diagonal elements of P being zero, where P is defined in Section 3. See Section 8.

IFAIL = 12

The degrees of freedom for error, $n - k \leq 0$ (this is an unlikely error exit), or the estimated value of σ was 0 during an iteration.

7 Accuracy

The precision of the estimates is determined by TOL; see Section 5. As a more stable method is used to calculate the estimates of θ than is used to calculate the covariance matrix, it is possible for the least-squares equations to be of full rank but the $(X^T X)$ matrix to be too nearly singular to be inverted.

8 Further Comments

In cases when $ISIGMA \geq 0$ it is important for the value of SIGMA to be of a reasonable magnitude. Too small a value may cause too many of the winsorized residuals, i.e., $\psi(r_i/\sigma)$, to be zero or a value of $\psi'(r_i/\sigma)$, used to estimate the asymptotic covariance matrix, to be zero. This can lead to errors IFAIL = 8 or 9 (if INDW \neq 0), 10 (if INDW = 0) and 11.

G02HBF, G02HDF and G02HFF together carry out the same calculations as G02HAF but for user-supplied functions for ψ , χ , ψ' and u .

9 Example

The number of observations and the number of x variables are read in followed by the data. The option parameters are then read in (in this case giving Schweppe type regression with Hampel's ψ function and Huber's χ function and then using the 'replace expected by observed' option in calculating the covariances). Finally a set of values for the constants are read in.

After a call to G02HAF, $\hat{\theta}$, its standard error and $\hat{\sigma}$ are printed. In addition the weight and residual for each observation is printed.

9.1 Program Text

```
*      G02HAF Example Program Text
*      Mark 14 Revised. NAG Copyright 1989.
*      .. Parameters ..
INTEGER          NIN, NOUT
PARAMETER       (NIN=5,NOUT=6)
INTEGER          NMAX, MMAX
PARAMETER       (NMAX=8,MMAX=3)
*      .. Local Scalars ..
DOUBLE PRECISION CPSI, CUCV, DCHI, H1, H2, H3, SIGMA, TOL
INTEGER          I, IC, IFAIL, INDC, INDW, IPSI, ISIGMA, IX, J, M,
+               MAXIT, N, NITMON
*      .. Local Arrays ..
DOUBLE PRECISION C(MMAX,MMAX), RS(NMAX), THETA(MMAX), WGT(NMAX),
+               WORK(4*NMAX+MMAX*(NMAX+MMAX)), X(NMAX,MMAX),
+               Y(NMAX)
*      .. External Subroutines ..
EXTERNAL        GO2HAF, X04ABF
*      .. Executable Statements ..
WRITE (NOUT,*) 'G02HAF Example Program Results'
*      Skip heading in data file
READ (NIN,*)
CALL X04ABF(1,NOUT)
*      Read in number of observations and number of X variables
READ (NIN,*) N, M
WRITE (NOUT,*)
IF (N.GT.0 .AND. N.LE.NMAX .AND. M.GT.0 .AND. M.LE.MMAX) THEN
*      Read in X and Y
DO 20 I = 1, N
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      READ (NIN,*) (X(I,J),J=1,M), Y(I)
20  CONTINUE
*   Read in control parameters
      READ (NIN,*) INDW, IPSI, ISIGMA
*   Read in appropriate weight function parameters.
      IF (INDW.NE.0) READ (NIN,*) CUCV, INDC
      IF (IPSI.GT.0) THEN
          IF (IPSI.EQ.1) READ (NIN,*) CPSI
          IF (IPSI.EQ.2) READ (NIN,*) H1, H2, H3
          IF (ISIGMA.GT.0) READ (NIN,*) DCHI
      END IF
*   Set values of remaining parameters
      IX = NMAX
      IC = MMAX
      TOL = 0.5D-4
      MAXIT = 50
*   * Change NITMON to a positive value if monitoring information
*   is required *
      NITMON = 0
      SIGMA = 1.0D0
      DO 40 I = 1, M
          THETA(I) = 0.0D0
40  CONTINUE
      IFAIL = -1
*
      CALL G02HAF(INDW,IPSI,ISIGMA,INDC,N,M,X,IX,Y,CPSI,H1,H2,H3,
+              CUCV,DCHI,THETA,SIGMA,C,IC,RS,WGT,TOL,MAXIT,NITMON,
+              WORK,IFAIL)
*
      IF ((IFAIL.NE.0) .AND. (IFAIL.LT.7)) THEN
          WRITE (NOUT,99999) 'G02HAF fails, IFAIL = ', IFAIL
      ELSE
          IF (IFAIL.GE.7) THEN
              WRITE (NOUT,99999) 'G02HAF returned IFAIL = ', IFAIL
              WRITE (NOUT,*)
+              '          Some of the following results may be unreliable'
          END IF
          WRITE (NOUT,99998) 'Sigma = ', SIGMA
          WRITE (NOUT,*)
          WRITE (NOUT,*) '          THETA          Standard'
          WRITE (NOUT,*) '          errors'
          DO 60 J = 1, M
              WRITE (NOUT,99997) THETA(J), C(J,J)
60  CONTINUE
          WRITE (NOUT,*)
          WRITE (NOUT,*) '          Weights          Residuals'
          DO 80 I = 1, N
              WRITE (NOUT,99997) WGT(I), RS(I)
80  CONTINUE
      END IF
      END IF
      STOP
*
99999 FORMAT (1X,A,I2)
99998 FORMAT (1X,A,F10.4)
99997 FORMAT (1X,F12.4,F13.4)
      END

```

9.2 Program Data

G02HAF Example Program Data

```

8  3          : N  M

1. -1. -1. 2.1 : X1 X2 X3 Y
1. -1.  1. 3.6
1.  1. -1. 4.5
1.  1.  1. 6.1
1. -2.  0. 1.3
1.  0. -2. 1.9

```

```

1. 2. 0. 6.7
1. 0. 2. 5.5 : End of X1 X2 X3 and Y values

1 2 1 : INDW IPSI ISIGMA
3.0 0 : CUCV INDC (Only if INDW.ne.0)
1.5 3.0 4.5 : H1 H2 H3 (Only if IPSI.eq.2)
1.5 : DCHI (Only if IPSI.gt.0 .and. ISIGMA.gt.1)

```

9.3 Program Results

G02HAF Example Program Results

Sigma = 0.2026

THETA	Standard errors
4.0423	0.0384
1.3083	0.0272
0.7519	0.0311
Weights	Residuals
0.5783	0.1179
0.5783	0.1141
0.5783	-0.0987
0.5783	-0.0026
0.4603	-0.1256
0.4603	-0.6385
0.4603	0.0410
0.4603	-0.0462
